## Spring 2011 McNabb GDCTM Contest Geometry

## NO Calculators Allowed

1.	Hezy leaves home for work at 6:45am. He drives to the Green Line train station
	3 miles away at an average speed of 30 mph. After 8 minutes he boards the
	train for downtown. The train averages $45~\mathrm{mph}$ for its $9~\mathrm{mile}$ journey. After a $7~\mathrm{mph}$
	minute walk Hezy arrives at work. What time does Hezy arrive at work?

(A) 7:11am (B) 7:18am (C) 7:21am (D) 7:27am (E) 7:29am

2. How many arrangements of *REVERE* are there in which the first *R* occurs before the first *E*?

**(A)** 12 **(B)** 18 **(C)** 20 **(D)** 24 **(E)** 30

3. In a class, 2/3 of the students have brown eyes and 4/5 of the students have brown hair. If students with brown eyes are twice as likely to have brown hair as students who do not have brown eyes, what fraction of the class has neither brown eyes nor brown hair?

**(A)** 1/30 **(B)** 1/15 **(C)** 1/10 **(D)** 2/15 **(E)** 1/5

4. Let *m* and *n* be integers satisfying  $m^2 + n^2 = 50$ . The value of m + n must be

**(A)** -8 **(B)** -5 **(C)** 0

**(D)** 10 **(E)** cannot be uniquely determined

5. Out of a sphere of clay with diameter 12, Marty fashions two spheres of radius 3 and 5 respectively. Using all of the remaining clay Jennifer fashions a sphere. What is the diameter of Jennifer's sphere?

**(A)** 4 **(B)** 6 **(C)** 8 **(D)** 10 **(E)** 12

6. Let a, b, x, and y > 0. If x = by and y = ax find the value of  $\frac{a}{1+a} + \frac{b}{1+b}$ .

**(A)** 1 **(B)** a **(C)** b/a **(D)** 2 **(E)** 1/(a+b)

	<b>(A)</b> 9	<b>(B)</b> $4\sqrt{5}$	<b>(C)</b> $4\sqrt{6}$	<b>(D)</b> 10	<b>(E)</b> 11			
9.		(28,0), and $(8,15)$ . The at is the value of $a + b$ ?						
	<b>(A)</b> 16	<b>(B)</b> 17	<b>(C)</b> 18	<b>(D)</b> 19	<b>(E)</b> 20			
10.	A regular 52 card deck is well shuffled. What is the probability that both the top and bottom cards are aces?							
	<b>(A)</b> 1/26	<b>(B)</b> 1/52	<b>(C)</b> 3,	/221 (	<b>D)</b> 2/221	<b>(E)</b> 1/221		
11.	1. In two years a son will be one-third as old as his father was 2 years ago. eighteen years this son will be the same age as his father was 18 years ag How old is the son now?							
	<b>(A)</b> 10	<b>(B)</b> 12	<b>(C)</b> 14	<b>(D)</b> 16	<b>(E)</b> 18			
12.	In $\triangle ABC$ , point $D$ is on segment $\overline{AC}$ and point $E$ is on segment $\overline{AB}$ . Segments $\overline{BD}$ and $\overline{CE}$ are drawn, intersecting at piont $F$ . If $AE/EB=2/5$ and $EF/FC=3/7$ then the ratio $BF/FD$ is equal to							
	(A) 7/2 (B) 8/3 (C) 4 (D) 9/2 (E) cannot be determined uniquely							
13.	Triangle $ABC$ is inscribed in a circle and $AB = AC = 6$ . Point $D$ lies on $BC$ with $AD = 4$ . $AD$ is extended through $D$ to $E$ on the circle. Find $DE$ .							
	<ul><li>(A) 4</li><li>(B) 5</li><li>(C) 6</li><li>(D) 7</li><li>(E) cannot be uniquely determined</li></ul>							
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7. If n and m are positive integers and  $480n = m^2$ , what is the smallest possible

**(D)** 240

8. In an isosceles trapezoid with bases 6 and 16 a circle is inscribed (touching all

four sides of the trapezoid). What is the diameter of this circle?

**(E)** 480

value of *m*?

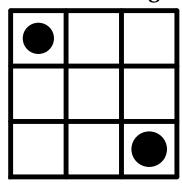
**(B)** 96

**(C)** 120

**(A)** 90

- 14. Recall that a Pythagorean triple is a triple (a, b, c) of positive integers satisfying  $a^2 + b^2 = c^2$ . Which of the following must be true?
  - (I.) At least one of *a*, *b*, and *c* must be odd
  - (II.) At least one of *a*, *b*, and *c* must be even
  - (III.) For at least one Pythagorean triple, a = b.
  - (A) I only
- **(B)** II only
- (C) I and II only
- **(D)** II and III only
- **(E)** none of them
- 15. Molly's Motel is adopting a new room key system. The new keys will be square  $3 \times 3$  cards each with two holes punched in them as in the figure. The two sides (what we would have called the front and back except we cannot tell which is which!) of such a card cannot be distinguished but there is a distinguished edge which is the edge to be inserted in the lock. What is the greatest number of rooms Molly's Motel can have?

insert this edge



- **(A)** 12
- **(B)** 18
- **(C)** 21
- **(D)** 24
- **(E)** 36
- 16. A train having to journey *x* miles in *h* hours, ran for *k* hours at a rate of *r* miles per hour, then stopped for *m* minutes. How fast must it go (in mph) on the rest of its journey to arrive on time?
- (A)  $\frac{x kr}{h k m}$  (B)  $\frac{x kr}{60h 60k m}$  (C)  $\frac{60(x kr)}{h k m}$  (D)  $\frac{60(x kr)}{h k 60m}$  (E)  $\frac{60(x kr)}{60h 60k m}$

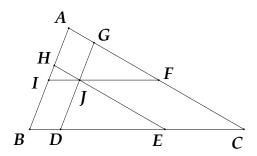
17. The series

$$1 \cdot 2 + 2 \cdot 3 + 3 \cdot 4 + \cdots + 100 \cdot 101$$

has the value

- **(A)** 333300
- **(B)** 343400
- **(C)** 353500
- **(D)** 363600
- **(E)** 404000
- 18. In a class of 28 students, 20 take Latin, 14 take Greek, and 10 take Hebrew. If no student takes all three languages and 6 take no language, how many students must be taking both Greek and Hebrew?
  - (A) cannot be uniquely determined
- **(B)** 0
- **(C)** 1

- (D) 2
- **(E)** 5
- 19. Ten coplanar lines are given such that (i) exactly three lines are parallel (each to the other two), (ii) no other pairs of lines are parallel, and (iii) no three lines are concurrent. How many triangles are formed by these ten lines?
  - **(A)** 64
- **(B)** 81
- **(C)** 87
- **(D)** 98
- **(E)** 100
- 20. In triangle *ABC* the transversals *DG*, *EH*, and *FI* are concurrent at *J*, with  $DG \parallel AB$ ,  $EH \parallel AC$ , and  $FI \parallel BC$ . If these three transversals have the same length, what is their common length if it is known that AB = 8, BC = 16, and CA = 12?



- **(A)** 91/13
- **(B)** 92/13
- **(C)** 94/14
- **(D)** 95/14
- **(E)** 96/13