## Fall 2014 McNabb GDCTM Contest Algebra Two

## NO Calculators Allowed

- 1. Fiji apples cost \$4.68 for a half-dozen and 90 cents a piece. Gala apples cost \$5.39 for a half-dozen and 97 cents a piece. If Sarah buys 8 Fiji apples and 9 Gala apples with a \$20 bill, how much change should she receive?
- 2. Forty-one erasers are distributed to *n* students. If at least one student always receives at least 6 erasers no matter how the erasers are distributed, what is the largest possible value of *n*?
- 3. Simplify

$$x - y - (3x - 4y) - (x - y - (3x - 4y))$$

- 4. The area of a rectangle is 864. The sum of the length and width is 60. By how much does the length exceed the width?
- 5. A regular hexagon is inscribed in a circle of radius one while another regular hexagon is circumcribed about this circle. What is the area of the region enclosed by the two hexagons?
- 6. How many arrangements of the letters in GDCTM do not have any 3 consecutive letters in alphabetical order? So, for instance, you would count DGCTM but you would not count DGCMT.
- 7. Solve the system

$$\begin{cases} \frac{x}{6} + \frac{4}{y} = 2\\ \frac{18}{x} + \frac{y}{2} = 5 \end{cases}$$
$$x - 3|x - 4| = |7 + 2x|$$

- 8. Solve:
- 9. Simplify  $\left(\sqrt{6}^{\sqrt{12}}\right)^{\sqrt{3}}$ .
- 10. What is the first time after 1pm that the minute and hour hand of a clock will overlap? Answer to the nearest second and express your answer in hours:minutes:seconds format.

1

11. In the diagram, segment *DB* is perpendicular to both *DF* and *AC*, and A - E - F are collinear. In addition, EF = 2AD. If  $\angle FAC$  measures 17° find the angle measure in degrees of  $\angle DAB$ .



- 12. The line y = mx intersects the lines x + y = 7 and x + y = -14 at points *A* and *B* respectively. If AB = 39, what is a possible value for the slope *m*?
- 13. Find the value of

$$\sum_{k=1}^{100} i^{k(k+1)/2}$$

Here, *i* stands for the square root of negative one.

- 14. Find the sum of the real roots of the polynomial  $x^4 16x^2 40x 25$ .
- 15. A regular six-pointed star, composed of two intersecting equilateral triangles each of side length  $6\sqrt{3}$ , is inscribed in a circle. Six congruent smaller circles are internally tangent to this circle and externally tangent to the star. Find the radius of the small circles.



2