## Fall 2016 McNabb GDCTM Contest Algebra One

## NO Calculators Allowed

- 1. Jerry has five times as many comic books as Tom. If Jerry has forty-five comic books, how many does Tom have?
- 2. Jane was born in the year 2003. When she was born, her Mom was 26 years old. In what year will Jane's Mom be three times older than her?
- 3. Simplify

$$5x^2 - 7x + 3 - 3(x+4)^2$$

- 4. John has some nickels and quarters, 37 coins in all. If the value of these coins is \$4.45, how many more nickels than quarters does John have?
- 5. If  $a \star b = \frac{a+b}{a+3b}$ , find the value of x that satisfies

$$2 \star (x \star 3) = 4$$

- 6. In how many ways can one arrange the letters of WINTER in such a way that the two vowels are never adjacent?
- 7. A theatre priced adult tickets to its play eight dollars higher than child tickets. At a certain performance, the theatre sold 75 more child tickets than adult tickets, for a total sales of \$1975. How much would the total sales have been if the prices of the child and adult tickets had been reversed?
- 8. How many zero's does the number 23! + 24! end in?
- 9. For how many integers k does the polynomial in x given by

$$4x^2 + kx - 9$$

factor over the integers?

- 10. Jorge has 57 coins with a total value of 90 cents. The coins are all pennies, nickels, or dimes. How many nickels does he have?
- 11. Six mathletes and two coaches sit at a circular table. If the two coaches sit across the table from each other, how many arrangements are possible?
- 12. Solve the system

$$\begin{cases} 13x + 14y = 15\\ 12x + 13y = 14 \end{cases}$$

13. What is the ten's digit of  $11^{2016}$ ?

14. Determine the sum of all the solutions of the equation

$$|x - 1| + |x| + |x + 1| = |4x|$$

15. If r and s are the roots of  $2x^2 = x + 10$ , find the value of  $r^2 + s^2$ .

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